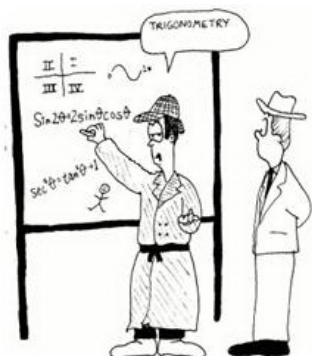


Trigonometric Equations

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What is a Trigonometric Equation?



The equations having trigonometric functions of unknown angles are known as [trigonometric equations](#).

For example: $\tan \theta = \frac{1}{\sqrt{3}}$

Solution of a trigonometric equation

The value of the unknown angle that satisfies the given trigonometric equation is called the [solution](#) of the trigonometric equation.

General Solutions of Trigonometric Equations

Under this section, we will learn about the [general solutions](#) of the trigonometric equations $\sin \theta = 0$, $\cos \theta = 0$, $\tan \theta = 0$ and $\cot \theta = 0$, $\sin \theta = \sin \alpha$, $\cos \theta = \cos \alpha$ and $\tan \theta = \tan \alpha$ and $a \cos \theta + b \sin \theta = c$

General Solution of $\sin \theta = 0$

The general solution of $\sin \theta = 0$ is $\theta = n\pi$, $n \in \mathbb{Z}$

General Solution of $\cos \theta = 0$

The general solution of $\cos \theta = 0$ is $\theta = (2n + 1)\frac{\pi}{2}$, $n \in \mathbb{Z}$.

General Solution of $\tan \theta = 0$

The general solution of $\tan \theta = 0$ is $\theta = n\pi$, $n \in \mathbb{N}$.

General Solution of $\cot \theta = 0$

The general solution of $\cot \theta = 0$ is $(2n + 1)\frac{\pi}{2}$, $n \in \mathbb{Z}$.

Important Note:

As we have discussed the general solution of 4 trigonometric ratios out of 6.

General Solution of $\sec \theta = 0$

Since $\sec \theta \geq 1$, or $\sec \theta \leq -1$

Therefore, $\sec \theta = 0$ does not have any solution.

General Solution of $\operatorname{cosec} \theta = 0$

Since $\operatorname{cosec} \theta \geq 1$, or $\operatorname{cosec} \theta \leq -1$

Therefore, $\operatorname{cosec} \theta = 0$ does not have any solution.

General Solution of $\sin \theta = \sin \phi$

$$\theta = n\pi + (-1)^n \phi, n \in \mathbb{Z}$$

The equation $\operatorname{cosec} \theta = \operatorname{cosec} \phi$ is equivalent to $\sin \theta = \sin \phi$. Thus, $\operatorname{cosec} \theta = \operatorname{cosec} \phi$ and $\sin \theta = \sin \phi$ have the same general solution.

General Solution of $\cos \theta = \cos \phi$

$$\theta = 2n\pi \pm \phi, \text{ where } n \in \mathbb{Z}.$$

The equation $\sec \theta = \sec \phi$ is equivalent to $\cos \theta = \cos \phi$. Thus, $\sec \theta = \sec \phi$ and $\cos \theta = \cos \phi$ have the same general solution.

General Solution of $\tan \theta = \tan \phi$

$$\theta = n\pi + \phi, n \in \mathbb{Z}$$

The equation $\tan \theta = \tan \phi$ is equivalent to $\cot \theta = \cot \phi$. Thus, $\tan \theta = \tan \phi$ and $\cot \theta = \cot \phi$ have the same general solution.

General Solution of $\sin^2 \theta = \sin^2 \phi$

$$\theta = n\pi \pm \phi, n \in \mathbb{Z}.$$

General Solution of $\cos^2 \theta = \cos^2 \phi$

$$\theta = n\pi \pm \phi, n \in \mathbb{Z}.$$

General Solution of $\tan^2 \theta = \tan^2 \phi$

$$\theta = n\pi \pm \phi, n \in \mathbb{Z}.$$

General Solution of $a \cos \theta + b \sin \theta = c$

$$a \cos \theta + b \sin \theta = c, \text{ where } a, b, c \in \mathbb{R} \text{ such that } c^2 \leq a^2 + b^2$$

In order to solve this type of equations, we reduce them in the form $\cos \theta = \cos \phi$ or $\sin \theta = \sin \phi$.

Now try it yourself! Should you still need any help, [click here](#) to schedule live online session with e Tutor!

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Reference Links:

- <http://www.purplemath.com/modules/solvtrig.htm>
- <http://www.wikihow.com/Solve-Trigonometric-Equations>
- http://en.wikibooks.org/wiki/Trigonometry/Solving_Trigonometric_Equations

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