## Graph of a Linear Equation in Two variables

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## Linear Equation in two variables



An equation of the form $a x+b y+c=0$ or $a x+b y=c$, where $a, b, c$ are real numbers, $a ? 0, b ? 0$ and $x, y$ are variables, is called $a$ linear equation in two variables.

Examples of linear equation in two variables :

- $x+2 y=1$
- $-2 x+3 y=4$


## Solution of Linear equation in two variables

Let $a x+b y+c=0$, where $a, b, c$ are real numbers, $a ? 0, b ? 0$. Then, any pair of values of $x$ and $y$ which satisfies the equation $a x$ $+b y+c=0$, is called asolution of it.

Example: $\mathrm{x}=3, \mathrm{y}=2$ is a solution of $3 \mathrm{x}-2 \mathrm{y}=5$ because when $\mathrm{x}=3$, $y=2$, we have: LHS $=3 \times 3-2 \times 2=5=$ RHS.

But, $x=3, y=-2$ is not its solution, because $3 \times 3-2 x(-2) ? 5$ i.e.
LHS ? RHS when $x=3$ and $y=-2$.

## Graph of a Linear Equation in two variables

In order to draw the graph of a linear equation $a x+b y+c=0, a ? 0$,
b? 0, we follow the steps written below :
Step I - Obtain the linear equation, Let the equation be $\mathrm{ax}+\mathrm{by}+\mathrm{c}=0$.

Step II - Express $y$ in terms of $x$ to obtain $y=\left(\frac{-a x+c}{b}\right)$

Step III - Give any two values to x and calculate the corresponding values of y from the expression in step II to obtain two solutions, say (?1,?1) and (?2, ?2).

If possible take values of x as integers in such a manner that the corresponding values of y are also integers.

Step IV - Plot points(?1,?1) and(?2, ?2) on a graph paper.

Step V - Join the points marked in step IV to obtain a line. The line obtained is the graph of the equation $a x+b y+c=0$.

## Important Remarks

(i) When a ? $0, \mathrm{c}$ ? 0 and $\mathrm{b}=0$

The equation $\mathrm{ax}+\mathrm{by}+\mathrm{c}=0$, reduces to $\mathrm{ax}+\mathrm{c}=0$ or $\mathrm{x}=-\mathrm{c} / \mathrm{a}$. In this case the graph of the equation $\mathrm{ax}+\mathrm{by}+\mathrm{c}=0$, is a straight line parallel to
$y-$ axis and passing through the point $(-c / a, 0)$
(ii) When b ? 0, c ? 0 and $\mathrm{a}=0$.

In this case, the equation $\mathrm{ax}+\mathrm{by}+\mathrm{c}=0$, is a straight line parallel to
$\mathrm{x}-$ axis and passing through the point $(0,-\mathrm{c} / \mathrm{b})$.
(iii) When a ? $0, \mathrm{~b}=0, \mathrm{c}=0$.

The equation $a x+b y+c=0$ reduces to $a x=0$ i.e. $x=0$. The graph of this equation is $y-a x i s$.
(iv) When $\mathrm{a}=0, \mathrm{~b} ? 0, \mathrm{c}=0$.

The equation $a x+b y+c=0$ reduces to by $=0$ i.e. $y=0$. The graph of this equation is $x-a x i s$.
(v) When $\mathrm{c}=0$.

The equation $a x+b y+c=0$ reduces to $a x+b y=0$. The graph of this equation is a line passing through the origin.
To get a more clear idea, let's explain with an example :

## Example : Draw the graph of the equation $\mathbf{y}-\mathrm{x}=2$.

We have, $\mathrm{y}-\mathrm{x}=2$
$y=x+2$
When $\mathrm{x}=1$, we have: $\mathrm{y}=1+2=3$
When $\mathrm{x}=3$, we have: $\mathrm{y}=3+2=5$
Thus, we have the following table exhibiting the abscissae and ordinates of points on the line represented by the given equation.

| $x$ | 1 | 3 |
| :---: | :---: | :---: |
| $y$ | 3 | 5 |

Plotting the points $(1,3)$ and $(3,5)$ on the graph paper and drawing a line joining them, we obtain the graph of the line represented
by the given equation as shown :


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## Reference Links :

- http://en.wikipedia.org/wiki/Linear_equation\#Linear_equations_in_two_variables
http://en.wikipedia.org/wiki/System_of_linear_equations

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