Graph of a Linear Equation in Two variables

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Linear Equation in two variables



An equation of the form ax + by + c = 0 or ax + by = c, where a,b, c are real numbers, a ? 0, b ? 0 and x, y are variables, is called a <u>linear equation in two variables</u>.

Examples of linear equation in two variables :

- $\mathbf{x} + 2\mathbf{y} = \mathbf{1}$
- -2x + 3y = 4

Solution of Linear equation in two variables

Let ax + by + c = 0, where a, b, c are real numbers, a ? 0, b ? 0. Then, any pair of values of x and y which satisfies the equation ax + by + c = 0, is called a<u>solution</u> of it.

Example: x = 3, y = 2 is a solution of 3x - 2y = 5 because when x = 3, y = 2, we have: LHS = $3 \times 3 - 2 \times 2 = 5 =$ RHS.

But, x = 3, y = -2 is not its solution, because $3 \times 3 - 2 \times (-2)$? 5 i.e. LHS ? RHS when x = 3 and y = -2.

Graph of a Linear Equation in two variables

In order to draw the graph of a linear equation ax + by + c = 0, a ? 0, b ? 0, we follow the steps written below :

Step I – Obtain the linear equation, Let the equation be ax + by + c = 0.

Step II – Express y in terms of x to obtain $y = \begin{bmatrix} -\frac{ax + c}{b} \end{bmatrix}$

Step III – Give any two values to x and calculate the corresponding values of y from the expression in step II to obtain two solutions, say (?1,?1) and (?2,?2).

If possible take values of x as integers in such a manner that the corresponding values of y are also integers.

Step IV – Plot points(?1,?1) and(?2, ?2) on a graph paper.

Step V – Join the points marked in step IV to obtain a line. The line obtained is the graph of the equation ax + by + c = 0.

Important Remarks

(i) When a ? 0, c ? 0 and b = 0

The equation ax + by + c = 0, reduces to ax + c = 0 or x = -c/a. In this case the graph of the equation ax + by + c = 0, is a straight line parallel to

y – axis and passing through the point (-c/a, 0)

(ii) When b ? 0, c ? 0 and a = 0.

In this case, the equation ax + by + c = 0, is a straight line parallel to x - axis and passing through the point (0, -c/b).

(iii) When a ? 0, b = 0, c = 0.

The equation ax + by + c = 0 reduces to ax = 0 i.e. x = 0. The graph of this equation is y - axis.

(iv) When a = 0, b ? 0, c = 0.

The equation ax + by + c = 0 reduces to by = 0 i.e. y = 0. The graph of this equation is x - axis.

(v) When c = 0.

The equation ax + by + c = 0 reduces to ax + by = 0. The graph of this equation is a line passing through the origin.

To get a more clear idea, let's explain with an example :

Example : Draw the graph of the equation y - x = 2.

We have, y - x = 2

$$y = x + 2$$

When x = 1, we have: y = 1 + 2 = 3

When x = 3, we have: y = 3 + 2 = 5

Thus, we have the following table exhibiting the abscissae and ordinates of points on the line represented by the given equation.

×	1	3
У	3	5

Plotting the points (1, 3) and (3, 5) on the graph paper and drawing a line joining them, we obtain the graph of the line represented

by the given equation as shown :



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Reference Links :

- http://en.wikipedia.org/wiki/Linear_equation#Linear_equations_in_two_variables
- http://en.wikipedia.org/wiki/System_of_linear_equations

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