

#### Point of intersection and concurrency of lines

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# **Point of Intersection of Two Lines**

```
Let the equations of two lines be
```

```
a1x + b1y + c1 = 0 - (i)

a2x + b2y + c2 = 0 - (ii)
```

Suppose these two lines intersect at a point P(x1, y1). Then, (x1, y1) satisfies each of the given equations.

Therefore, a1x1 + b1y1 + c1 = 0 and a2x-1 + b2y1 + c2 = 0

Solving these two by cross multiplication, we get

```
x1 = y1 = 1

b1c2 - b2c1 c1a2 - c2a1 a1b2 - a2b1

x1 = b1c2 - b2c1

a1b2 - a2b1

y1 = c1a2 - c2a1

a1b2 - a2b1
```

Hence, the coordinates of the point of intersection of (i) and (ii) are:

```
b1c2 - b2c1 , c1a2 - c2a1

a1b2 - a2b1   a1b2 - a2b1
```

### **Important Remark**

1. To find the coordinates of the point of intersection of two non - parallel lines, we solve the given equations simultaneously and the values of x and y so obtained determine the coordinates of the point of intersection.

#### **Condition of Concurrency of three lines**

Three lines are said to be concurrent if they pass through a common point i.e. they meet at a point.

Thus, if three lines are concurrent the point of intersection of two lines lies on the third line. Let

```
a1x + b1y + c1 = 0 - (i)

a2x + b2y + c2 = 0 - (ii)

a3x + b3y + c3 = 0 - (iii)

be three concurrent lines.
```

Then the point of intersection of (i) and (ii) must lie on the third. The coordinates of the point of intersection of (i) and (ii) are

```
b1c2 - b\neg2c1, c1a2 - c2a1

a1b2 - a2b1 a1b2 - a2b1

This point must lie on (iii)

Therefore, a3 b1c2 - b\neg2c1 + b3 c1a2 - c2a1 + c3 = 0

a1b2 - a2b1 a1b2 - a2b1

a3(b1c2 - b2c1) + b3(c1a2 - c2a1) + c3(a1b2 - a2b1) = 0

a1 b1 c1

a2 b2 c2 = 0
```

This is the required condition of concurrency of three lines.

## Another condition of concurrency of three lines

Three lines: L1  $\Box$  a1x + b1y + c1 = 0 L2  $\Box$  a2x + b2y + c2 = 0 L3  $\Box$  a3x + b3y + c3 = 0 are concurrent iff there exist constants ?1, ?2, ?3 not all zero such that ?1L1 + ?2L2 + ?3L3 = 0 ?1 (a1x + b1y + c1) + ?2 (a2x + b2y + c2) + ?3 (a3x + b3y + c3) = 0

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#### **Reference Links:**

- http://en.wikipedia.org/wiki/Intersection
- http://en.wikipedia.org/wiki/Cross-multiplication
- <a href="http://en.wikipedia.org/wiki/Concurrent\_lines">http://en.wikipedia.org/wiki/Concurrent\_lines</a>

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