Point of intersection and concurrency of lines

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Point of Intersection of Two Lines

Let the equations of two lines be a1x + b1y + c1 = 0 - (i)a2x + b2y + c2 = 0 - (ii)Suppose these two lines intersect at a point P(x1, y1). Then, (x1, y1) satisfies each of the given equations. Therefore, a1x1 + b1y1 + c1 = 0 and $a2x\neg 1 + b2y1 + c2 = 0$ Solving these two by cross multiplication, we get x1 = y1 = 1 b1c2 - b2c1c1a2 - c2a1a1b2 - a2b1x1 = b1c2 - b2c1a1b2 - a2b1 $y_1 = c_1a_2 - c_2a_1$ a1b2 - a2b1

Hence, the coordinates of the point of intersection of (i) and (ii) are: b1c2 - b2c1, c1a2 - c2a1a1b2 - a2b1 a1b2 - a2b1

Important Remark

1. To find the coordinates of the point of intersection of two non - parallel lines, we solve the given equations simultaneously and the values of x and y so obtained determine the coordinates of the point of intersection.

Condition of Concurrency of three lines

Three lines are said to be concurrent if they pass through a common point i.e. they meet at a point.

Thus, if three lines are <u>concurrent</u> the point of intersection of two lines lies on the third line. Let

a1x + b1y + c1 = 0 - (i)a2x + b2y + c2 = 0 - (ii)a3x + b3y + c3 = 0 - (iii)be three concurrent lines.

Then the point of intersection of (i) and (ii) must lie on the third. The coordinates of the point of intersection of (i) and (ii) are b1c2 - b-2c1, c1a2 - c2a1a1b2 - a2b1 a1b2 - a2b1

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Therefore, a3 b1c2 - b\neg2c1 + b3 c1a2 - c2a1 + c3 = 0
a1b2 - a2b1 a1b2 - a2b1
a3(b1c2 - b2c1) + b3(c1a2 - c2a1) + c3(a1b2 - a2b1) = 0
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a1 b1 c1 a2 b2 c2 = 0

Another condition of concurrency of three lines

Three lines: L1 \square a1x + b1y + c1 = 0 L2 \square a2x + b2y + c2 = 0 L3 \square a3x + b3y + c3 = 0 are concurrent iff there exist constants ?1, ?2, ?3 not all zero such that ?1L1 + ?2L2 + ?3L3 = 0 ?1 (a1x + b1y + c1) + ?2 (a2x + b2y + c2) + ?3 (a3x + b3y + c3) = 0

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Reference Links :

- http://en.wikipedia.org/wiki/Intersection
- http://en.wikipedia.org/wiki/Cross-multiplication
- <u>http://en.wikipedia.org/wiki/Concurrent_lines</u>

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