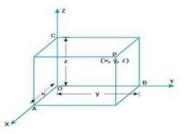


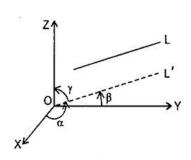
# **Direction Cosines and Direction Ratios of a Line**

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# Introduction



We have already learned the basic concepts of vectors. In this topic we will use the concepts of vector algebra to the three dimensional geometry. In the three dimensional geometry, we deal with direction cosines, direction ratios, equations of line in space, equation of plane in space etc.



## **Direction Cosines**

If a directed line L' passing through the origin makes angles ?, ? and ? with x, y and z axes respectively then cosine of these angles namely,

cos?, cos? and cos? are called <u>direction cosines</u> of the directed line L'.

Usually the direction cosines are denoted by l, m and n

1=cos?, m=cos? and n=cos?

#### Relation between the direction cosines of a line

If l, m and n are the direction cosines of a line then  $l^2 + m^2 + n^2 = 1$ 

Also, 
$$\cos^2 ? + \cos^2 ? + \cos^2 ? = 1$$

#### Direction cosines of a line passing through two points

Let  $P(x_1, y_1, z_1)$  and  $Q(x_2, y_2, z_2)$  be two points on a line L, then

$$PQ = ?((x_2-x_1)^2 + (y_2-y_1)^2 + (z_2-z_1)^2)$$

Direction cosines of the line L is given by,  $\frac{x_2-x_1}{PQ}$ ,  $\frac{y_2-y_1}{PQ}$ ,  $\frac{z_2-z_1}{PQ}$ 

## **Direction Ratios of a line**

Any three numbers which are proportional to the direction cosines of a line are called <u>direction ratios</u> of the line. If l, m and n are direction cosines abd a, b and c are direction ratios of a line then a=?l, b=?m and c=?n.

$$I = m = n = \lambda$$

It can also be written as a b c

If  $P(x_1, y_1, z_1)$  and  $Q(x_2, y_2, z_2)$  are any two points the direction ratios of PQ is given by  $\langle x_2 - x_1, y_2 - y_1, z_2 - z_1 \rangle$ 

#### Direction cosines of x, y and z-axis

X-axis makes angles 0?, 90? and 90? with itself, so the direction cosines are  $\cos 0$ ?,  $\cos 90$ ? and  $\cos 90$ ? = <1, 0, 0>

Y-axis makes angles 90?, 0? and 90? with itself, so the direction cosines are cos90?, cos0? and cos90? = <0, 1, 0>

Z-axis makes angles 90?, 90? and 0? with itself, so the direction cosines are cos90?, cos90? and cos0? = <0, 0, 1>

### **Condition for collinearity**

If a<sub>1</sub>, b<sub>1</sub>, c<sub>1</sub> and a<sub>2</sub>, b<sub>2</sub>, c<sub>2</sub> are the direction cosines of line joining two points then the points are said to be collinear

$$a_1 = b_1 = c_1$$
  
if  $a_2 b_2 c_2$ 

**Example:** Find the direction cosines of a line which makes equal angles with the coordinate axes.

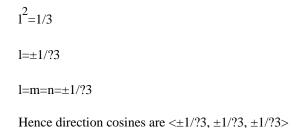
**Solution:** Given ? = ? = ?, so cos? = cos? = cos?

l=m=n

$$1^2 + m^2 + n^2 = 1$$

$$1^2 + 1^2 + 1^2 = 1$$

$$31^2 = 1$$



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#### **Reference Links:-**

- http://en.wikipedia.org/wiki/Direction\_cosine
- http://www.solitaryroad.com/c400.html
- <a href="http://en.wikipedia.org/wiki/Three-dimensional\_space">http://en.wikipedia.org/wiki/Three-dimensional\_space</a>

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