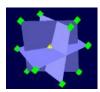


Various forms of a Plane

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Plane - Introduction



A plane can be determined uniquely if anyone of the following is known:

- (i) The normal to the plane and its distance from origin is given.
- (ii) It passes through a point and is perpendicular to a given direction.
- (iii) It passes through three given non collinear points.

Equation of plane in normal form

Vector Form: If r is the position vector of a point P in the plane, d is the perpendicular distance from origin and? is the unit normal to the plane then its vector equation is given by

$$r. ? = d$$

Cartesian Form: If P(x, y, z) is a point in the plane, d is the perpendicular distance from origin and <l, m, n> are the direction cosines of ?, then the Cartesian form of the plane is given by

$$lx + my + nz = d$$

Note: If $\langle a, b, c \rangle$ are the direction ratios of the normal to the plane then the equation is ax + by + cz = d

Equation of a plane perpendicular to a given vector and passing through a given point

Vector Form: If \overline{a} is the position vector of a given point and \overline{N} is the perpendicular vector then its equation is given by $(\overline{r}, \overline{a})$. $\overline{N}=0$

Cartesian Form: If A(x1, y1, z1) is the given point and P(x, y, z) is a general point in the plane and A, B and C are the direction ratios of \overline{N} then the Cartesian equation is given by

$$A(x-x_1)+B(y-y_1)+C(z-z_1)=0$$

Equation of a plane passing through three non collinear points

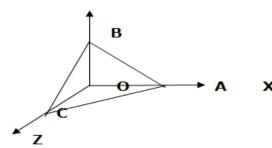
Vector Form: If \bar{a} , \bar{b} and \bar{c} are the position vectors of three points and \bar{r} be any point in the plane, then the <u>equation of the plane</u> passing through three given points is

$$(r-a).[(b-a)X(c-a)]=0$$

Cartesian Form: If (x1, y1, z1), (x2, y2, z2) and (x3, y3, z3) are the three given points then equation of the plane is

$$\begin{vmatrix} x-x_1 & y-y_1 & z-z_1 \\ x_2-x_1 & y_2-y_1 & z_2-z_1 \\ x_3-x_1 & y_3-y_1 & z_3-z_1 \end{vmatrix} = 0$$

Intercept Form of a plane



If the plane makes intercepts a, b and c on x, y and z axes respectively

then its equation in intercept form is given by

$$\begin{array}{ccccc}
x + y + z & = & 1 \\
- & - & - \\
a & b & c
\end{array}$$

Here coordinates of A, B and C are A(a,0,0), B(0,b,0) and C(0,0,c) respectively.

Intersection of two planes

Vector Form: If \vec{r} , $\vec{n}_1 = d_1$ and \vec{r} , $\vec{n}_2 = d_2$ are the vector equation of two planes then equation of the plane passing through the intersection of these two planes is given by

$$r.(\bar{n}_1+?\bar{n}_2)=d_1+?d_2$$

Cartesian Form: If $A_1x+B_1y+C_1z=d_1$ and $A_2x+B_2y+C_2z=d_2$ are the equations of two planes in the Cartesian form then the equation of the plane passing through the intersection of the given planes is

$$(A_1x+B_1y+C_1z-d_1)+?(A_2x+B_2y+C_2z-d_2)=0$$

In general, if P_1 and P_2 are the equations of two planes then the equation of the plane passing through the intersection of P_1 and P_2 is given by

$$P_1+?P_2=0$$

Example: Find the equation of the plane through the intersection of the planes x+y+z-6=0 and 2x+3y+4z+5=0 ant the point (1, 1, 1)

Solution: Equation of the plane passing through x+y+z-6=0 and 2x+3y+4z+5=0 is given by

$$(x+y+z-6) + ? (2x+3y+4z+5)=0$$
(1)

Passes through (1, 1, 1)

$$(1+1+1-6) + ? (2+3+4+5) = 0$$

?=3/14

Substitute the value of ? in (1), so that the equation is

$$(x+y+z-6)+3/14(2x+3y+4z+5)=0$$

20x+23y+26z-69=0, which is the required equation.

Now try it yourself! Should you still need any help, click here to schedule live online session with e Tutor!

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Reference links:

- http://en.wikipedia.org/wiki/Plane_%28geometry%29
- http://en.wikipedia.org/wiki/Surface_normal
- http://www.cs.fit.edu/~wds/classes/cse5255/thesis/planeEqn/planeEqn.html
- http://www.wikidoc.org/index.php/Plane_%28mathematics%29
- http://mathworld.wolfram.com/Plane.html

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