

EQUALITY OF TWO MATRICES

Created: Thursday, 24 November 2011 13:11 | Published: Thursday, 24 November 2011 13:11 | Written by Super User | Print

Equality of two Matrices



Two matrices $A = [a_{ij}]$ and $B = [b_{ij}]$ are said to be equal if they are of same order and each element of A is equal to the corresponding element of B, that is $a_{ij} = b_{ij}$ for all i and j. Symbolically we write it as A = B

For example: If
$$(x + 3 + 2y - 7)$$
 = $\begin{pmatrix} 0 & 6 & 3y - 2 \\ -6 & a - 1 & 0 \\ b - 3 & -21 & 0 \end{pmatrix}$ = $\begin{pmatrix} 0 & 6 & 3y - 2 \\ -6 & -3 & 2c + 2 \\ 2b + 4 & -21 & 0 \end{pmatrix}$

Find the values of a, b, c, x, y and z

Solution: Since the matrices are equal, corresponding elements are equal

$$x + 3 = 0$$

$$x = -3$$

$$z + 4 = 6$$

$$z = 2$$

$$2y - 7 = 3y - 2$$

$$2y - 3y = -2 + 7$$

$$y = -5$$

$$a - 1 = -3$$

$$a = -2$$

$$2c + 2 = 0$$

$$c = -1$$

$$b - 3 = 2b + 4$$

$$b - 2b = 7$$

$$b = -7$$

Hence, a = -2, b = -7, c = -1, x = -3, y = -5 and z = 2.

Try this:

1. Given that the following matrices are equal, find the values of x and y.

$$A = \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix}$$
$$B = \begin{pmatrix} x & 2 \end{pmatrix}$$

(Answer: x = 1, y = 4)

2. Given that the following matrices are equal, find the values of x, y, and z.

A =
$$\begin{pmatrix} 4 & 0 \\ 6 & -2 \\ 3 & 1 \end{pmatrix}$$

B = $\begin{pmatrix} x & 0 \\ 6 & y + 4 \\ z / 3 & 1 \end{pmatrix}$

(Answer: x = 4, y = -6, and z = 9)

Construction of a Matrix

When the general term and the order of a matrix is given, we can easily construct a matrix.

For example: Construct a 3 x 4 matrix whose elements are given by $a_{ij} = 2i - j$

$$a11 = 2 - 1 = 1$$
 $a12 = 2 - 2 = 0$ $a13 = 2 - 3 = -1$ $a14 = 2 - 4 = -2$ $a21 = 4 - 1 = 3$ $a22 = 4 - 2 = 2$ $a23 = 4 - 3 = 1$ $a24 = 4 - 4 = 0$ $a31 = 6 - 1 = 5$ $a32 = 6 - 2 = 4$ $a33 = 6 - 3 = 3$ $a34 = 6 - 4 = 2$

$$A = \begin{pmatrix} 1 & 0 & -1 & -2 \\ 3 & 2 & 1 & 0 \\ 5 & 4 & 3 & 2 \end{pmatrix}$$

Now try it yourself! Should you still need any help, <u>click here</u> to schedule live online session with e Tutor!

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Reference Links:

- http://en.wikipedia.org/wiki/Matrix (mathematics)
- http://www.mathreference.com/la-mpoly,order.html
- http://wiki.answers.com/Q/What_is_order_of_the_resultant_matrix_AB_when_two_matrices_are_multiplied_and_the_order_of_the_

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